

프란시스 수차 모델 내 흡출관의 내부 유동 특성에 미치는 공기 주입구의 영향

모하메드 아부 사저^{*,**} · 김승준^{*} · 조 용^{***} · 김진혁^{*,**†}

Effect of Air Injection Holes Intrusiveness on Internal flow Phenomena of a Draft Tube Inside a Francis Turbine Model

Mohammad Abu Shahzer^{*,**}, Seung-Jun Kim^{*}, Yong Cho^{***}, Jin-Hyuk Kim^{*,**†}

Key Words : Swirling flow(스윙 유동), Draft tube(흡출관), Air-injection holes(공기 인젝션 홀), Francis turbine(프란시스 수차)

ABSTRACT

Swirling flow inside draft tube at part load condition during cavitation inception induces large pressure fluctuations. For suppression of the draft tube surge, fins with air injection holes are employed on the draft tube wall. The protrusion of air injection holes obstructs the incoming flow and creates flow complexities near the holes. The present study transiently investigates the effect of protrusion of these holes on the performance and flow phenomena of the Francis turbine numerically. Reynolds averaged Navier-Stokes (RANS) equations are solved along with a two-phase mixture model using Scale Adaptive Simulation Shear Stress Transport (SAS-SST) model to solve the turbulent flows. The numerical methodology is then verified by an experiment based on the International Standard (IEC 60193) norms. The hole protrusion reduces the efficiency of the turbine and exhibits higher strength of the vortex rope which is minimized using fins without holes. The swirl number is reduced by about 34% for the draft tube without holes. The random pressure fluctuations caused by the hole's intrusiveness are also suppressed when the holes are removed.

1. Introduction

Part load (PL) conditions are designated by lower flowrate (Q) operating conditions. The downstream swirl instabilities at this condition contribute to the higher losses in the draft tube (DT).⁽¹⁾ Because of the significant runner exit circumferential velocity at PL condition, a helical precessing vortex is generated called vortex rope. In the runner rotation direction, these vortex ropes rotate with a precession frequency of about 0.2 to 0.4 times the rotational frequency of the runner.⁽²⁾ The vortex rope is a significant

contributor to the DT flow instabilities which are responsible for vibration and pounding noise.⁽³⁾ The turbine may fail catastrophically because of the DT surge when the vibrational frequency matches the natural frequency of the structure.

In the Francis turbine cavitation is a very common phenomenon that results in noise and vibration in the draft tubes. At PL condition cavitation can take place inside the vortex rope which further increases the amplitude of the pressure fluctuations at the DT wall. Hence the turbine may fail due to resonance as well as due to pitting of the material.⁽⁴⁾

* 한국생산기술연구원 탄소중립산업기술연구부문 (Carbon Neutral Technology R&D Department, Korea Institute of Industrial Technology)

** 과학기술연합대학원대학교 융합제조시스템공학 (청정공정·에너지시스템공학) 전공 (Convergence Manufacturing System Engineering (Green Process and Energy System Engineering), University of Science & Technology)

*** 한국수자원공사 K-water 융합연구원 (K-water Convergence Institute, Korea Water Resources Corporation)

† 교신저자, E-mail : jinhyuk@kitech.re.kr

The nature of the DT flow induces the low-frequency instabilities which disrupt the stable and safe operation of the turbine so, to suppress this DT surge various techniques have been developed. There are three main control approaches for dealing with the pressure changes caused by the cavitating vortex rope; stabilizer fins mounted on the DT wall, air or water injection, and runner cone extension.⁽⁵⁾ These strategies have virtues in terms of reducing the surge, but they also have flaws. Given other physical design restrictions on turbines, extending the runner cone can be prohibitive. Insufficient air supply keeps the vortex rope unhindered and the natural frequency may decrease which leads to the resonance.⁽⁶⁾ Muntean et al.⁽⁷⁾ discovered that when the turbine works at a reduced discharge, the dynamic behaviour is severely harmed by the air injection control mechanism. Also, air or water admission frequently necessitates the use of more electricity.

Installing fins in the entrance cone of a draft tube is a popular method of reducing pressure surges. It is an intrusive type of mitigation strategy which decreases the high swirl content in the outlying zone of the DT since it is mounted on the DT circumference parallelly in the flow direction. Nishi et al.⁽⁸⁾ used wall pressure pulses to evaluate the influence of fins on the half load surging and suggested that triangular fins are more effective than square ones. Mounted fins, on the other hands, were discovered to be prone to significant efficiency losses, cavitation erosion, and the ability to enhance structural vibrations.

Taking into account the combination of characteristics, some researchers used both fins and air admission approaches, called hybrid control, to alleviate the draft tube surge.^(9,10) In this hybrid control, holes on the surface of a fin or on the runner crown are used to allow air in. Kim et al.⁽¹⁰⁾ investigated numerically the effect of anti-swirl fins along with air injection from runner crown for which they considered four fins. Cylindrical holes are protruded from the surfaces of the fins inside the DT in their model. At PL condition without considering cavitation, they discovered that the control methodology significantly reduces the pressure pulsation and the operation range is broadened for the Francis turbine. But, the intrusion portion of the injection holes obstructs the incoming

flow and some complex flow phenomenon takes place which was not elaborated by the researchers.

Conclusively, the utilization of fins along with the air injection technique greatly mitigate the DT synchronous pressure pulsations. The obstruction created by the injection holes in the DT flow induces flow complexity and randomness near the hole surface which could be detrimental to the safe working of the Francis turbine. Therefore, a thorough investigation is needed for the explanation of the physics behind these complex flows. To address this important issue of the control techniques, the current study investigates numerically the effect of air injection hole protrusion inside the DT on the pressure pulsation. The operating condition is selected at PL condition with cavitation for the same geometrical model used by Kim et al.⁽¹⁰⁾. The anti-swirl fins with and without air injection holes are considered for the study but the air injection technique is not taken into account. A transient numerical investigation is carried out for the accurate prediction of the flow complexities. The experimental investigation is also performed for the numerical validation.

2. Geometrical model

The present numerical study utilizes the three-dimensional (3-D) geometry of the Francis turbine model. The turbine model consists of stationary components; spiral casing, stay vanes, guide vanes and a draft tube as well as rotating component; runner. The basic function of the draft tube is to guide the runner exit flow and convert the excess kinetic energy (KE) into static pressure. The DT has two diffusers for better conversion. The full geometrical model is shown in Fig. 1 in which a zoomed-in view of the anti-swirl fins is also depicted. There are four fins mounted on the DT out of which two are long fins placed opposite to each other and two fins are short fins that are also placed diagonally. At each fin, one air injection hole (red colour in Fig. 1) is generated which is protruded inside the DT and acts as an obstruction in the flow. The holes are situated at a location of $0.09 D_2$ from the DT inlet. In general, the flow gets obstructed by the fin's geometry but due to the intrusive nature of the holes the incoming flow gets more deflected and flow

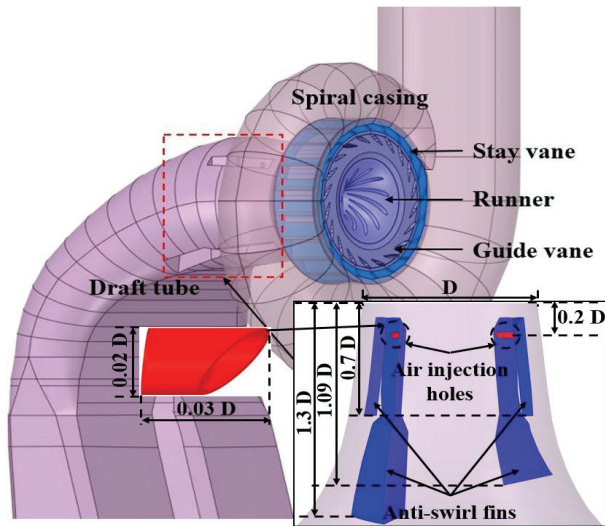


Fig. 1 3D geometrical model of the Francis turbine

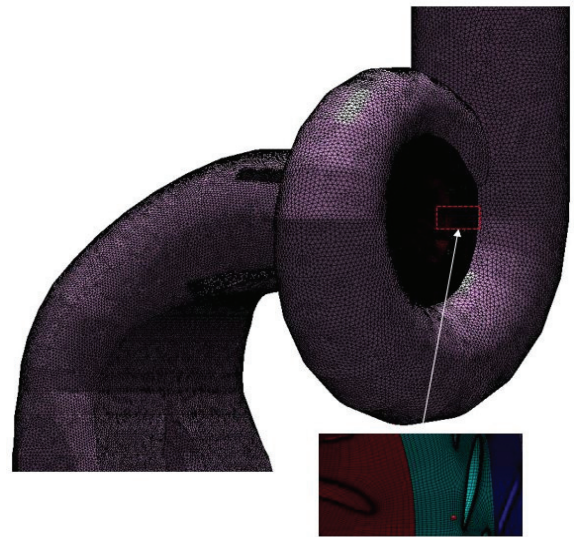


Fig. 2 Computational grid on the turbine model

Table 1 Turbine specifications and operating conditions

Parameters	Value
Number of guide vanes	20
Number of stay vanes	20
Number of runner blades	11
DT inlet diameter, D_2 (m)	0.35
Specific speed, N_s (rpm,kW,m)	276
Energy coefficient E_{nD}	3.34
Guide vane angle	16°
Speed factor n_{ED}	0.541
Discharge factor Q_{ED}	0.223
Thoma number σ	0.266

exhibits unsteadiness near the holes.

The operating condition for the turbine is set at a lower flowrate for which $Q/Q_{BEP}=0.74$ (BEP–Best efficiency point) that lies between the range of flowrate which exhibits severe downstream instabilities. For the cavitating vortex rope, cavitation condition is also incorporated in this study. The cavitation phenomenon is quantified by a non-dimensional quantity called Thoma number (σ). The σ depends on the suction head of the turbine, so by regulating pressure at the DT outlet, the suction head is created for which the cavitation initiates. This condition is termed cavitation inception and the value of $\sigma=0.266$ in the current investigation. Hence, the pressure pulsation with and without holes is transiently investigated at PL condition with cavitation inception point. The specifications of the Francis turbine model are tabulated in Table 1. The coefficients

definitions in Table 1 can be referenced in ref.⁽¹¹⁾

3. Numerical methodology

The internal flow physics is predicted using the commercial software ANSYS CFX in the present numerical study. Since the flow in the turbine is turbulent and transient in nature, the physics of this flow is captured by solving unsteady Reynolds averaged Navier Stokes (URANS) equations assuming the flow is incompressible. The closure problem of the URANS equations is treated by the scale adaptive simulation shear stress transport (SAS–SST) model which precisely captures the vortical flows in the Francis turbine.⁽¹²⁾ To model the cavitation a widely accepted two–phase Rayleigh–Plesset model is employed.⁽¹³⁾ The numerical solution needs discrete points so grids are generated on the turbine model. For spiral casing and DT, a tetrahedral mesh is generated while for other components hexahedral mesh is employed. The runner is a spinning component so the y^+ value for this is kept below 5. The mesh independency is handled by a technique called Grid convergence index (GCI) for which three meshes are generated; fine, medium and coarse.⁽¹⁴⁾ For these meshes discretization errors are calculated. For fine mesh with 8.95×10^6 grid elements, the GCI values of efficiency and flowrate are 0.0091 and 0.0093. Since these values are below 0.01 so the fine mesh is considered for further investigations. The generated grids on the turbine model are depicted in

Table 2 Boundary conditions

Boundary conditions	Value
Operating fluid	Water and vapor at 25 C
Interface	Transient rotor stator
Time step	0.0002083 s
Total time	0.249996 s
Loop coefficient	5

Fig. 2.

The physical components of the turbine are merged with the interfaces. The rotating and stationary domains are connected with General Grid Interface (GGI). The boundary conditions are specified in Table 2. The boundary condition for the inlet of the spiral casing is mass flow rate and the static pressure is applied at the DT outlet for the cavitation inception. No-slip and automatic wall functions are applied at the turbine's wall. The unsteady cavitating flow is solved by initializing the solutions by steady cavitating solutions which are also initialized by steady non-cavitating solutions. Hence, the transient investigation has better convergence. The time step is calculated for the 1.5° of runner rotation and five full runner revolutions are considered for the solution.

4. Results and discussions

4.1 Numerical validation

The developed numerical methodology for the Francis turbine model is validated with the experimental data which is obtained from the IEC 60193 standard based experimentation. For the verification of performance characteristics of the turbine, steady results are utilized at $n_{ED}=0.467$ with the variation of guide vane openings from 16° to 26°. The experiment is performed on the model having anti-swirl fins with air injection holes. Figure 3 shows the validation of efficiency and power and these are in good agreement with the experimental results. The efficiency and power are normalized using the BEP values of the experiment.

4.2 Unsteady hydraulic performance

To analyse the effect of air injection hole protrusion

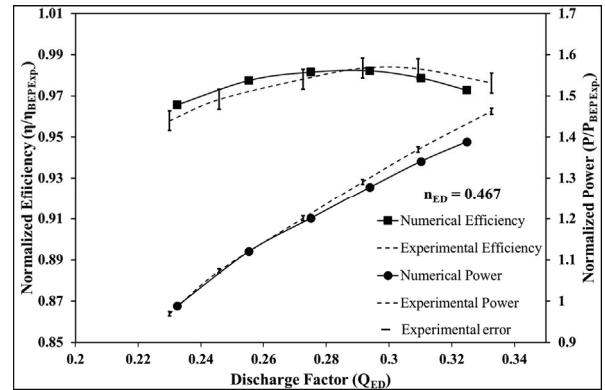


Fig. 3 Performance validation of the turbine model

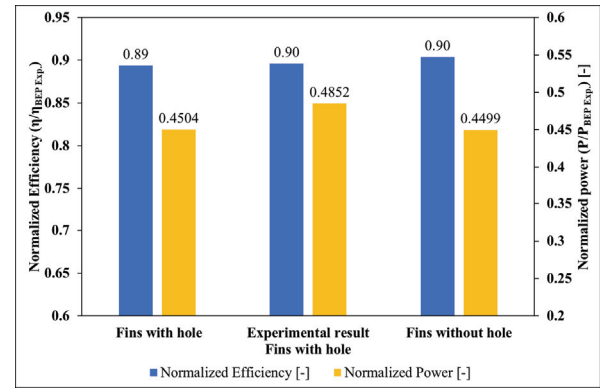


Fig. 4 Performance characteristics of the turbine model

on the hydraulic performance, efficiency and power are calculated using the unsteady methodology for with and without holes cases. At PL with cavitation inception point, the numerical and experimental performance curves are depicted in Fig. 4. The experimental results are obtained for the turbine which has holes protruded on its DT. The efficiency and power are non-dimensionalized using the experimental BEP results. With holes on the fin's surfaces, the numerical performances are in good agreement with the experimental results as shown in Fig. 4. Because of the smoother flows near the fins, the efficiency attains an increased value for the DT without air injection holes compared to with holes case. However, the numerical power for both cases shows insignificant variation.

In order to justify the efficiency increment in the without holes case, the DT head loss is calculated for both the cases using eq. (1).⁽¹⁰⁾

$$H_{loss} = \frac{\Delta p}{\rho g} \quad (1)$$

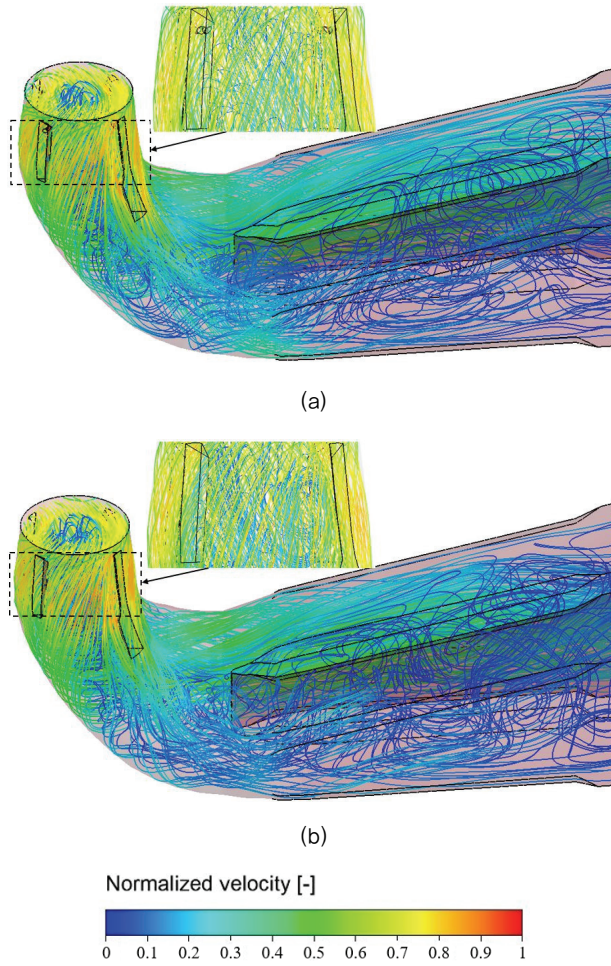


Fig. 5 Velocity streamline distributions (a) Fins with holes (b) Fins without holes

where Δp is the pressure difference between inlet and outlet of the draft tube domain, ρ is the density of the fluid and g is the gravitational acceleration. The loss percentage is calculated by normalizing the head loss by the effective head at PL condition. It is found that for the DT having fins with air injection holes, the head loss is 9.34% while the DT without holes exhibits lesser head loss of 8.8%. Hence, it is clear that the hole's protrusion creates more flow complexities with unsteadiness which contribute to the efficiency reduction.

4.3 Internal flow phenomena

The evaluation of complex internal flow characteristics of the turbine model is essential for the prediction of the effect of the air injection hole protrusion. The accurate flow field visualization is

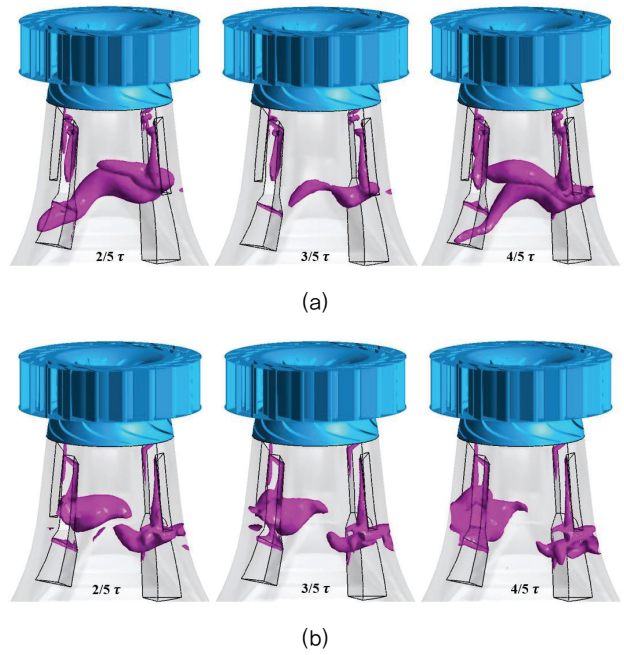


Fig. 6 Iso-surface distribution of pressure ($p=p_{sat}$) (a) Fins with holes (b) Fins without holes

obtained through velocity streamlines for both the cases as shown in Fig. 5. The plots are obtained by averaging the velocity for the last two runner revolutions and then normalized by the maximum velocity. It can be observed from Fig. 5 that the DT with and without holes attain almost a constant velocity value. However, near the holes a slight increase of velocity can be seen in Fig 5(a) with flow non-uniformity compared to without holes case in Fig 5(b). The recirculating flow has occurred for both the cases at the DT centre resulting in the vortex rope generation. The circumferential momentum pushes the flow towards the larger curvature of the elbow of the DT. Improper kinetic energy conversion is achieved at this operating condition caused by the PL vortex rope and cavitation for both cases. Thus, hole protrusion causes more non-uniformity near the holes which plays a role in the improper energy conversion.

The cavitating vortex rope inside the DT can induce large pressure fluctuations and the operating range of the turbine is minimized. So, in the present study accurate prediction of the vortex rope is presented through Iso-surface distribution of pressure which is shown in Fig. 6. The Iso-surfaces are plotted for three instants (τ) during the last runner revolution. The boundary-value of pressure for these plots is set at the saturation pressure (p_{sat}) of the water. From this

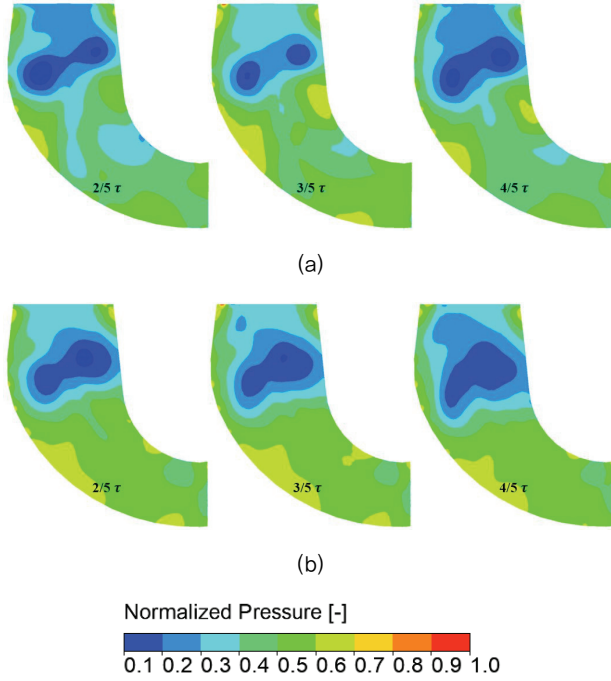


Fig. 7 Static pressure contours at the mid-section of DT
(a) Fins with holes (b) Fins without holes

figure, a large vortex rope can be observed inside the DT with air injection holes at the fin's surface. A significant reduction in the vortex rope strength is obtained for the without holes case. The precession direction of the vortex rope is the same as that of the runner's rotational direction. A low-pressure zone is found for both the cases which are attached to the upper part of the fins at all the instants. Because of the increased velocity near the holes, the area of this low-pressure zone is increased which contributed to the complex flows near the holes while without holes case does not show such adverse characteristics. Overall, longer and wider vortex rope is induced with holes compared to without holes case. Hence, the swirl instabilities are comparatively enhanced.

The static pressure contours inside the DT are also plotted at the mid-section for three instances to validate the vortex rope plots in Fig. 7. The pressure is normalized using maximum pressure and the lowest pressure value corresponds to the saturation pressure of the water. It can be noted from Fig. 7 that the low pressure occurs for both the cases in the form of random lobes because the vortex rope is non-uniform across the mid-section of the DT (Figure 6). Draft tube with hole exhibits higher area for low-pressure zone compared to without holes case which is indicative of

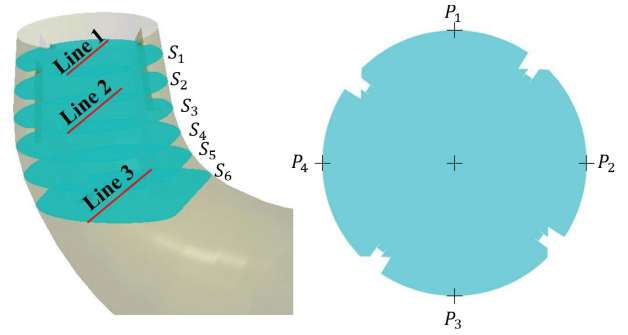


Fig. 8 Monitoring points, line and planes

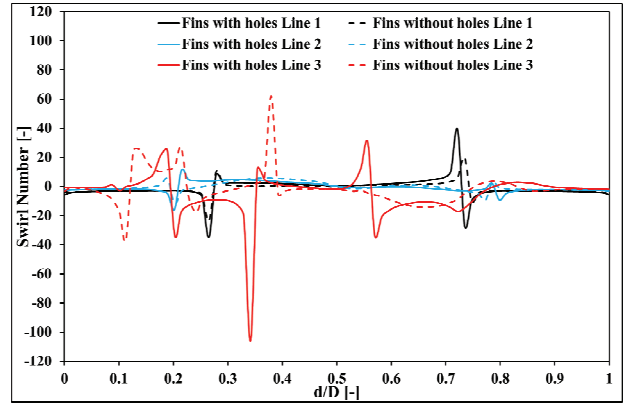


Fig. 9 Swirl number at Line 1 inside the DT

increased downstream instabilities. The lower pressure zones are entrapped in the cone portion of the DT so the induced flow complexities are more in this area only.

4.4 Swirl strength and pressure fluctuations

The swirl strength and pressure fluctuations are an important integral for the thorough investigation of the PL and cavitation induced instabilities. Figure 8 shows the monitoring points, lines and planes for which these parameters are calculated. There are six planes (S1 to S6) in the DT flow direction and at each plane, four points (P1 o P4) on the DT wall are monitored. The swirl intensity is represented using a non-dimensional number called swirl number (S) which is mathematically represented by eq. (2) and the unknowns notations can be found in ref.⁽¹⁰⁾;

$$S = \frac{\int_0^R C_m \cdot C_u \cdot r^2 \cdot dr}{R \int_0^R C_m^2 \cdot r \cdot dr} \quad (2)$$

The swirl number is calculated at line 1, line 2 and

line 3 which lie on the planes S_1 , S_3 and S_6 respectively using statistical averaged circumferential and axial velocities as shown in Fig. 9. In this figure, 0 and 1 denote two opposite points on the DT circumference. Since the vortex rope is not regular, the swirl number is also showing the same behaviour. The variation in the swirl number can be seen at two points which are on either side of the DT centre. The DT without air injection holes is clearly showing lesser swirl strength compared to the DT with holes for all the lines in the flow direction. The maximum swirl intensity is obtained at line 3 as the axial component of the velocity becomes very low in the downstream direction of the DT. The decrement in the maximum values of the swirl number for without holes case is about 40.29%, 25.26% and 41.66% at lines 1, 2 and 3 respectively. Hence, the hole protrusion significantly increased the swirl

intensity which further reduce the working range of the Francis turbine.

The pressure fluctuations are essential for the design point of view of the turbine. Fast Fourier transforms (FFT) methodology is employed to calculate the pressure pulsations on the DT wall at PL and cavitation inception point as shown in Fig. 10. The pressure amplitudes are obtained at P_1 since maximum fluctuations occur at this point only. The amplitude is normalized using the maximum value during the calculation and the frequency (f) is normalized using runner rotational frequency (f_n). The PL caused vortex rope generally induces low-frequency pressure fluctuations. From Fig. 10(a) for the DT with holes, the low-frequency pressure peak can be observed at each point in the DT flow direction. These pressure peaks occur for the frequency range of 0.2 to 0.4 f_n . Apart from the low-frequency peak, a random pressure peak is obtained at 3 f_n beyond which the pressure pulsations are showing the normal trend. As the holes are removed from the fin's surface, this random pressure fluctuation is significantly suppressed as shown in Fig. 10(b). However, a slight increase in the low-frequency peak can also be observed from this figure. Therefore, it is proved that the random pressure pulsation at 3 f_n occurs due to the presence of air injection holes protrusion inside the DT due to which the turbine's operating range is limited.

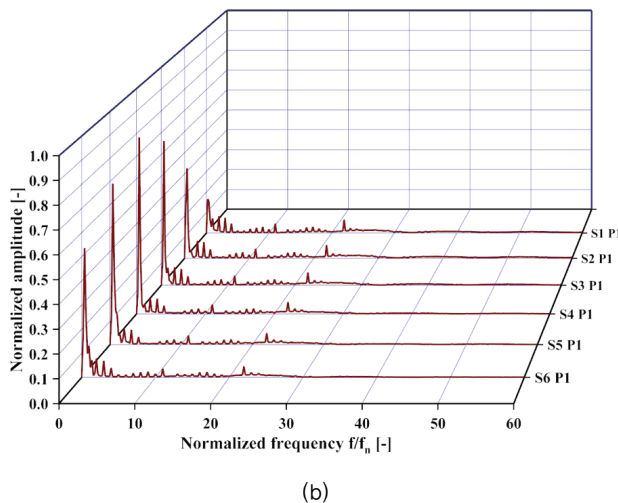
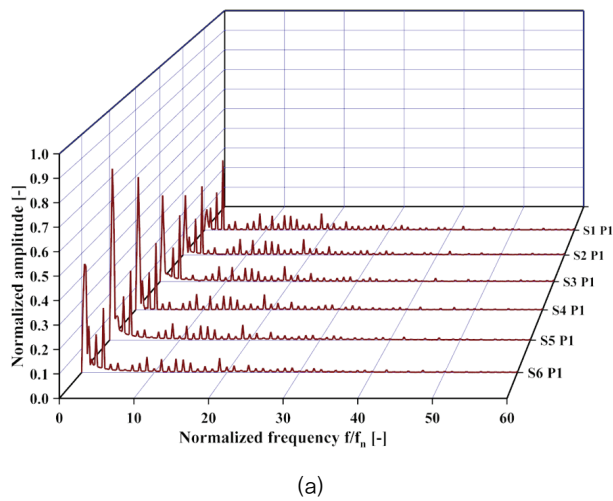


Fig. 10 Pressure pulsations (a) Fins with holes (b) Fins without holes

5. Conclusion

The present study investigates the effect of protrusion of air injection holes in the DT flow which are attached to the fins. These holes obstruct the incoming flow and induce some random complexities. The accurate calculations of the performances and internal flow characteristics of the turbine with and without holes are performed using the unsteady numerical methodology. The effect of these holes was investigated at PL condition incorporating the cavitation inception point at $\sigma=0.266$. It was found that the protrusion of the air injection holes reduces the efficiency by about 1% compared to the without holes case by creating some complex flows near the holes. The non-uniformity caused by these holes is the result of longer and wider vortex rope which is

minimized by removing the holes. Also, significant low-pressure zones are attached to the fin's holes which are reduced for the case of without holes. The maximum swirl intensity inside the DT is reduced by about 41% for the DT without holes which will lead to the stable operation of the turbine. Finally, random pressure pulsations at a higher frequency are the results of the hole's protrusion which is remarkably suppressed for without holes case. Furthermore, this study can be utilized for the optimization of the holes and fin's shape.

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